Homework 2 (version 2): (PHY249 Plasma Accelerator Physics, Fall 2021, Tajima) Deadline: Oct. 19 Monday, 2021, 5pm to <u>ttajima@uci.edu</u> (cc: to Greg: <u>huxtablg@uci.edu</u>) (Your collaboration among your colleagues is encouraged. If you work together to work out the homework, please show your colleagues' names together in your submission. (If you wish to submit your homework answer collectively together as a group, that is also OK with showing on who are your co-authors. If you have any questions, feel free to ask me).

A.

Argue why higher the (longitudinal) plasma wave phase velocity v_{ph} is, it is more robust. Show which plasma electrons are trapped [ref. T. O'Neil, Phys. Plasma **8**, 2255 (1965)] by such a wave whose trapping width is v_{tr} . Then, derive the Tajima-Dawson field $E_{TD} = m \omega_p c / e$ when you set v_{tr} is the ultimate phase velocity of $v_{ph} = c$.

Β.

Show that if you set the wakefield phase velocity lower than the speed of light c, say at v_{ph} , then we obtain the saturation field E_{ph} of wakefield as $E_{ph} = E_{TD}(v_{ph} / c)$.

(Your derivation may be either mathematical, or verbal, or their mixture).